

MA1023-Mathematical Methods-S2-2014-Mid-Make up	Field:
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Q2:

- a) The random variable Y is defined such that $Y = 0.6X_1 + 0.4X_2$ where X_1 = weight of boxes manufactured and X_2 = volume of the same boxes. If $E(X_1) = 5$, $E(X_1^2) = 34$, $E(X_2) = 3$, $E(X_2^2) = 18$ and $\text{Cov}(X_1, X_2) = 0.8$ find the standard deviation of Y .

- b) If the pdf of random variable is such that $f(x) = \begin{cases} x + 1 & \text{for } -1 \leq x < 0 \\ 1 - x & \text{for } 0 < x < 1 \\ 0 & \text{otherwise} \end{cases}$, find the cumulative distribution function, $F_X(x)$.

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Q3. Solve the differential equation $\frac{dy}{dx} - \frac{y}{x} = 1 - e^{-x}$, $y(1) = 0$ representing $y = y(x)$ as an integral.

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Q4. Let $y(x)$ be the solution to the differential equation in Q3. Find $\lim_{x \rightarrow \infty} \frac{y(x)}{x}$.

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Q5. In the calculation of the volume of a cube of nominal size 10", the uncertainty in the measurement of each side is 12%. The uncertainty in the measurement of the volume would be

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Q6. The root of the equation $f(x) = 0$ is found by using secant method. Given one of the initial estimates is $x_0 = 3$ and $f(3) = 5$, and the angle the secant makes with the function $f(x)$ is 57° , the next estimate of the root, x_1 , is